

Chapter 14: Control theory: graphical techniques

ML_14_1 Root locus

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%
% Chapter 14: Control theory: graphical techniques: Root Locus Techniques
%
% Example 14.1: MATLAB allows root loci to be plotted with the
% rlocus(GH) command, where  $G(s)H(s) = \text{numgh}/\text{dengh}$  and GH is an LTI
transfer-
% function object. Points on the root locus can be selected interactively
% using the  $[K,p] = \text{rlocfind}(GH)$  command. MATLAB then yields the gain(K)
at
% that point as well as all other poles(p) that have that gain. We can zoom
% in and out of the root locus by changing the range of axis values using
% the command  $\text{axis}([xmin,xmax,ymin,ymax])$ . The root locus can be drawn
% over a grid that shows constant damping ratio(z) and constant natural
% frequency( $\omega_n$ ) curves using the  $\text{sgrid}(z,\omega_n)$  command. To plot multiple
% z and  $\omega_n$  curves, use  $z = zmin:zstep:zmax$  and  $\omega_n = \omega_{nmin}:\omega_{nstep}:\omega_{nmax}$ 
to
% specify a range of values.

'Example 14.1'          % Display label.
clf                    % Clear graph on screen.
%numgh=[1 -4 20];      % Define numerator of G(s)H(s).
%dengh=poly([-2 -4]);  % Define denominator of G(s)H(s).
%numgh=[1 1.5];        % Define numerator of G(s)H(s).
%dengh=poly([0 -1 -10]); % Define denominator of G(s)H(s).
numgh=[1 4];           % Define numerator of G(s)H(s).
dengh=[0 -1 -2 -6];   % Define denominator of G(s)H(s).
'G(s)H(s)'            % Display label.
GH=tf(numgh,dengh)    % Create G(s)H(s) and display.
rlocus(GH)            % Draw root locus.
z=0.2:0.05:0.5;       % Define damping ratio values: 0.2 to
                      % 0.5 in steps of 0.05.
wn=0:1:10;            % Define natural frequency values: 0
                      % to 10 in steps of 1.
sgrid(z,wn)           % Generate damping ratio and natural
                      % frequency grid lines for root
                      % locus.
title('Root Locus')  % Define title for root locus.
pause
rlocus(GH)            % Draw close-up root locus.
axis([-3 1 -4 4])    % Define range on axes for root locus
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% close-up view.
title('Close-up')      % Define title for close-up root
                        % locus.
%z=0.45;              % Define damping ratio line for
z=0.8;                % Define damping ratio line for
                        % overlay on close-up root locus.
wn=0;                 % Suppress natural frequency overlay
                        % curves.
sgrid(z,wn)           % Overlay damping ratio curve on
                        % close-up root locus.
for k=1:3              % Loop allows 3 points to be selected
                        % as per Example 8.7
                        % (z=0.45, jw crossing, breakaway).
[K,p]=rlocfind(GH)    % Generate gain, K, and closed-loop
                        % poles, p,
                        % for point selected interactively on
                        % the root locus.
end                    % End loop.
pause

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